

0.2.7)  $y = e^{rx}$   
 $y' = r e^{rx}$   
 $y'' = r^2 e^{rx}$

$\Rightarrow e^{rx} (r^2 + 2r - 8) = 0$ ,  $r^2 + 2r - 8 = (r+4)(r-2)$

$\uparrow$  Needs to be 0 so this is 0 for  $r = 2, -4$

1.1.10) Just integrate,  $x = C + \frac{t^2}{2} + \int \sin(t^2) dt$  but for I.C.,

$\leadsto x = 20 + \frac{t^2}{2} + \int_0^t \sin(\Delta^2) d\Delta$

or could just have

$x = 20 + \int_0^t (\Delta + \sin(\Delta^2)) d\Delta$

1.2.4)  $f(x, y) = \frac{xy}{\cos x}$  and  $\frac{\partial f}{\partial y}(x, y) = \frac{x}{\cos x}$ . Also  $x_0 = 0, y_0 = 1$ .

•  $f$  is continuous as long as  $\cos x \neq 0 \Leftrightarrow x \neq \pm \frac{\pi}{2}, \pm \frac{3\pi}{2}, \dots$

Near our I.C.  $x_0 = 0, y_0 = 1$ , we are not <sup>at</sup> these bad pts so  $f$  is continuous near the I.C. ( $x_0 = 0, y_0 = 1$ ).

•  $f_y$  is continuous near the I.C. for the same reason.

Thus Picard's Thm  $\Rightarrow$  Implies a solution exists & it is unique.

Thus, it's possible to find a solution  $\checkmark$

1.3.10) we first read as  $y' = \frac{e^{-y}}{x}$  separate  $\frac{dy}{e^{-y}} = \frac{dx}{x} \cdot \left( \frac{1}{e^{-y}} \text{ is } e^{+y} \right)$ .

Note:  $x \neq 0$ . Integrating,  $\int e^y dy = \int \frac{dx}{x} \leadsto \boxed{e^y = \ln|x| + C}$  General Implicit Soln

I.C.  $y(1) = 1 \Rightarrow e^1 = \ln(1) + C$ , so  $\boxed{C = e}$ . Also, since  $x = 1$  to start, choose positive branch of  $\ln(+x)$ .

Thus,  $e^y = \ln(x) + e$  undo e  $\leadsto \boxed{y = \ln(\ln(x) + e)}$ .

For inside ln:  $x > 0$  and  $\ln(x) + e > 0 \Rightarrow \ln(x) > -e$ ;  $\boxed{x > e^{-e}}$  is our domain.