

# COMPLEX ANALYSIS, HW # 4

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Section 7, problems 41, 47, 49, 69, 72 and these problems:

## Problem 1.

Let  $K \subset \mathbb{C}$  be a compact set. Prove that  $u(z) = -\log(\text{dist}(z, K))$  is a subharmonic function in  $\mathbb{C} \setminus K$ .

## Problem 2.

Let  $h(z)$  be a  $C^2$  function in a neighborhood of the closed unit disc. Prove that inside the unit disc  $h$  can be represented as a difference of two subharmonic functions.