

# Laplace Transform Review Table

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| $f(t)$                       | $\mathcal{L}\{f(t)\} = F(s)$                    |
|------------------------------|-------------------------------------------------|
| $C$                          | $C/s$                                           |
| $t^n \ (n = 1, 2, 3, \dots)$ | $n!/s^{n+1}$                                    |
| $e^{-at}$                    | $1/(s+a)$                                       |
| $\sin(\omega t)$             | $\omega/(s^2 + \omega^2)$                       |
| $\cos(\omega t)$             | $s/(s^2 + \omega^2)$                            |
| $\sinh(\omega t)$            | $\omega/(s^2 - \omega^2)$                       |
| $\cosh(\omega t)$            | $s/(s^2 - \omega^2)$                            |
| $u(t-a)$                     | $(e^{-as})/s$                                   |
| $\delta(t-a)$                | $e^{-as}$                                       |
| $g'(t)$                      | $sG(s) - g(0)$                                  |
| $g''(t)$                     | $s^2G(s) - sg(0) - g'(0)$                       |
| $g'''(t)$                    | $s^3G(s) - s^2g(0) - sg'(0) - g''(0)$           |
| $f(t-a)u(t-a)$               | $e^{-as}\mathcal{L}\{f(t)\}$                    |
| $f(t)u(t-a)$                 | $e^{-as}\mathcal{L}\{f(t+a)\}$                  |
| $(f * g)(t)$                 | $\mathcal{L}\{f(t)\} \cdot \mathcal{L}\{g(t)\}$ |
| $e^{-at}f(t)$                | $F(s+a)$                                        |
| $\int_0^t f(\tau) d\tau$     | $\frac{1}{s}F(s)$                               |
| $-tf(t)$                     | $F'(s)$                                         |

For the bottom 3 rows of the table, assume  $\mathcal{L}\{f(t)\} = F(s)$ .