Chapter 7, problems 10, 11, 12, 17, 19, 23, and this problem:

Problem 1.

Let u(z) be harmonic in $D =: D(0,1) \setminus \{0\}$ such that

$$\lim_{z \to 0} \frac{u(z)}{\log |z|} = 0.$$

Prove that u can be extended to be harmonic in D(0, 1).