# INTRO DIFFERENTIAL EQUATIONS

Final Exam 1

Wednesday, December 10, 2008 — 8:00 am - 10:00 am

Problem	1	2	3	4	5	Σ
Points						

Student's name:

# Problem 1.

Find a bounded solution of the differential equation

$$\frac{dy}{dt} = y + \sin t.$$

# Problem 2.

Compute the first three Picard iterates  $(y_0(t),y_1(t),$  and  $y_2(t))$  for the initial value problem

$$\frac{dy}{dt} = t - y^2, \quad y(0) = 0.$$

### Problem 3.

Solve the initial value problem

$$y'' + 3y' + 2y = 1 + H_1(t), \ y(0) = 0, \ y'(0) = 0,$$

where

$$H_1(t) = \begin{cases} 0, & t < 1, \\ 1, & t \ge 1. \end{cases}$$

# Problem 4.

Check that  $y_1(t)=t$  and  $y_2(t)=\frac{t^2+t+1}{t+1}$  are solutions of the equation  $(t^2-1)y''+4ty'+2y=6t.$ 

Find the general solution.

# Problem 5.

Find the general solution of the system of equations

$$\begin{cases} \frac{dx_1}{dt} = 2x_1 - x_2 + x_3\\ \frac{dx_2}{dt} = x_1 + 2x_2 - x_3\\ \frac{dx_3}{dt} = x_1 - x_2 + 2x_3 \end{cases}$$