

Given a binary relation  $R$  from  $A$  to  $B$  and sets  $X \subseteq A$  and  $Y \subseteq B$ , we define:

- (a)  $R[X] = \{y \in B \mid (\exists x \in X)(x, y) \in R\}$
- (b)  $\text{rng}(R) = R[A] = \{y \in B \mid (\exists x \in A)(x, y) \in R\}$
- (c)  $R^{-1}[Y] = \{x \in A \mid (\exists y \in Y)(x, y) \in R\}$
- (d)  $\text{dom}(R) = R^{-1}[B] = \{x \in A \mid (\exists y \in B)(x, y) \in R\}$ .