

### Homework 11 (additional problems)

Introduction to Probability - MATH/STATS 425, Winter 2012

1. Random variables  $X$  and  $Y$  are jointly distributed according to the joint pdf

$$f(x, y) = \begin{cases} k \sin(x + y) & \text{for } 0 \leq x \leq \pi/2, 0 \leq y \leq \pi/2 \\ 0 & \text{eslewhere.} \end{cases}$$

- (a) Find the coefficient  $k$ .
- (b) Find the marginal pdf's of  $X$  and  $Y$ .
- (c) Find the conditional pdf of  $X$  given  $Y = y$ .
- (d) Find the expected value of  $X$ .
- (e) Find the conditional expectation of  $X$  given  $Y = y$ .