

SOLUTIONS

Quiz 7, March 7, 2012

Introduction to Probability - MATH/STATS 425, Winter 2012

Blood pressure of adults is normally distributed with mean 110 and standard deviation 10. Blood pressure is classified as normal if falls within 110 ± 12.8 range. Two adults come for an office visit independently from each other. What is the probability that at least one of them has an *abnormal* blood pressure?

(You may round off the table values to the first leading digit. For example, round off .7834 to .8)

Let $X =$ blood pressure of a random adult.
 $X \sim N(110, 10^2)$.

- $P\{\text{normal pressure}\} = P\{110 - 12.8 \leq X \leq 110 + 12.8\}$
 $= P\left\{-1.28 \leq \frac{X - 110}{10} \leq 1.28\right\}$
 $= \Phi(1.28) - \Phi(-1.28)$
 $= 2\Phi(1.28) - 1 \approx 2 \times 0.9 - 1 = 0.8$.
- $P\{\text{both patients have normal pressure}\} = 0.8^2 = 0.64$ (by independence).
- $P\{\text{at least one has abnormal pressure}\} = 1 - 0.64 = 0.36$