Math2E - Practice Final

June 2, 2008

1. Evaluate $\int \int_R (x-y)/(x+y) dA$, where R is the region with vertices (0, 2), (1, 1), (2, 2), and (1, 3).

2. Evaluate $\int_C xy dx + y dy$, C is the sine curve $y = \sin x, 0 \le x \le \pi/2$.

- 3. $\mathbf{F}(x, y, z) = e^{y}\mathbf{i} + (xe^{y} + e^{z})\mathbf{j} + ye^{z}\mathbf{k}$, (a): Show that \mathbf{F} is conservative,

 - (b): Evaluate $\int_C \mathbf{F} \cdot d\mathbf{r}$, where C is the line segment from (0, 2, 0) to (4, 0, 3).

4. Evaluate $\int_C x^2 y dx + \ln \sqrt{1+y^2} dy$, where C is the triangle from (0,0) to (2,2) to (0,2) to (0,0).

5. Evaluate $\int \int_S \mathbf{F} \cdot \mathbf{n} dS$, where $\mathbf{F}(x, y, z) = x^2 \mathbf{i} + xy \mathbf{j} + z \mathbf{k}$ and S is the part of the paraboloid $z = x^2 + y^2$ below the plane z = 1 with upward orientation.

6. Evaluate $\int \int_S \operatorname{curl} \mathbf{F} \cdot \mathbf{n} dS$, where $\mathbf{F}(x, y, z) = x^2 y z \mathbf{i} + y z^2 \mathbf{j} + z^3 e^{xy} \mathbf{k}$, S is the part of the sphere $x^2 + y^2 + z^2 = 5$ that lies above the plane z = 1, and S is oriented upward.

7. Evaluate $\int_C \mathbf{F} \cdot d\mathbf{r}$, where $\mathbf{F}(x, y, z) = xy\mathbf{i} + yz\mathbf{j} + zx\mathbf{k}$ and C is the triangle with vertices (1, 0, 0), (0, 1, 0), and (0, 0, 1), oriented counterclockwise as viewed above.

8. Evaluate $\int \int_S \mathbf{F} \cdot \mathbf{n} dS$, where $\mathbf{F}(x, y, z) = x^3 \mathbf{i} + y^3 \mathbf{j} + z^3 \mathbf{k}$ and S is the surface of the solid bounded by the cylinder $x^2 + y^2 = 1$ and the planes z = 0 and z = 2.